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# Coexistence of short- and long-range ferromagnetic order in nanocrystalline $\text{Fe}_2\text{Mn}_{1-x}\text{Cu}_x\text{Al}$ ( $x=0.0, 0.1$ and $0.3$ ) synthesized by high-energy ball milling

Tran Dang Thanh<sup>a,\*</sup>, Dwi Nanto<sup>b</sup>, Ngo Thi Uyen Tuyen<sup>c</sup>, Wen-Zhe Nan<sup>d</sup>, YiKyung Yu<sup>e</sup>, Daniel M. Tartakovsky<sup>e,\*</sup>, S.C. Yu<sup>d,\*</sup>

<sup>a</sup> Institute of Materials Science, Vietnam Academy of Science and Technology, 18 Hoang Quoc Viet, Hanoi, Vietnam

<sup>b</sup> Physics Education, Syarif Hidayatullah States Islamic University, Jakarta 15412, Indonesia

<sup>c</sup> Department of Natural Science, Nha Trang Pedagogic College, Nguyen Chanh, Nha Trang, Khanh Hoa, Vietnam

<sup>d</sup> Department of Physics, Chungbuk National University, Cheongju 361-763, Korea

<sup>e</sup> Department of Mechanical and Aerospace Engineering, University of California, San Diego, CA 92093-0411, USA

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## ABSTRACT

In this work, we prepared nanocrystalline  $\text{Fe}_2\text{Mn}_{1-x}\text{Cu}_x\text{Al}$  ( $x=0.0, 0.1$  and  $0.3$ ) powders by the high energy ball milling technique, and then studied their critical properties. Our analysis reveals that the increase of Cu-doping concentration (up to  $x=0.3$ ) in these powders leads to a gradual increase of the ferromagnetic–paramagnetic transition temperature from 406 to 452 K. The Banerjee criterion suggests that all the samples considered undergo a second-order phase transition. A modified Arrott plot and scaling analysis indicate that the critical exponents ( $\beta=0.419$  and  $0.442$ ,  $\gamma=1.082$  and  $1.116$  for  $x=0.0$  and  $0.1$ , respectively) are located in between those expected for the 3D-Heisenberg and the mean-field models; the values of  $\beta=0.495$  and  $\gamma=1.046$  for  $x=0.3$  sample are very close to those of the mean-field model. These features reveal the coexistence of the short- and long-range ferromagnetic order in the nanocrystalline  $\text{Fe}_2\text{Mn}_{1-x}\text{Cu}_x\text{Al}$  powders. Particularly, as the concentration of Cu increases, values of the critical exponent shift towards those of the mean-field model. Such results prove the Cu doping favors establishing a long-range ferromagnetic order.

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## 1. Introduction

Heusler alloys are thought to have a wide range of thermoelectric [1,2], spintronics [3,4], and magnetocaloric [5–7] applications. This is because  $\text{Co}_2\text{MnSi}$  Heusler alloys are experimentally shown to be half-metallic; and the phenomenon of half-metallic magnetism plays a crucial role in magnetoelectronics and spintronics [8], both of which are at the forefront of modern nanoscience [9]. These alloys possess a giant tunneling magnetoresistance ratio of 570% that has been observed at 2 K in  $\text{Co}_2\text{MnSi}/\text{Al}-\text{O}/\text{Co}_2\text{MnSi}$  magnetic tunnel junction [10]. A half-metallic magnetic material exhibits a usual metallic behavior for the one spin direction, while an energy gap in the band structure is present in other spin directions similarly to semiconductors [11,12]. The borderline between magnetoelectronics and

spintronics is flexible [13].

Most studies of the magnetocaloric effect (MCE) in Heusler alloys deal with low temperatures not exceeding room temperature. Unfortunately, there are a few work reported for above room temperature. Among the few high-temperature studies, the MCE was observed in an  $\text{Ni}_{49}\text{Mn}_{39}\text{Sb}_{12}$  alloy at around 347 K (with the maximum magnetic entropy change  $|\Delta S_{\text{max}}|=5.2 \text{ J kg}^{-1} \text{ K}^{-1}$  under an applied magnetic field change  $H=50 \text{ kOe}$ ) [14] and in an  $\text{Ni}_{0.5}\text{Mn}_{0.3}\text{Sb}_{0.2}$  alloy at around 342 K (with  $|\Delta S_{\text{max}}|=1.0 \text{ J kg}^{-1} \text{ K}^{-1}$  under  $H=12 \text{ kOe}$ ) [15]. Even less attention has been paid to Fe-based Heusler alloys. A notable exception is the study of  $\text{FeMnGa}$  alloys [16], which found a strong hysteresis due to the fact that the martensitic phase induced by the applied field cannot be completely recovered to austenite when the magnetic field decreases to zero.

In this paper, we present a detailed analysis of critical properties near the ferromagnetic (FM)–paramagnetic (PM) phase transition of nanocrystalline  $\text{Fe}_2\text{Mn}_{1-x}\text{Cu}_x\text{Al}$  ( $x=0.0, 0.1$  and  $0.3$ ) powders by using the modified Arrott plots (MAP) [17], the

\* Corresponding authors.

E-mail addresses: [thanhxraylab@yahoo.com](mailto:thanhxraylab@yahoo.com) (T.D. Thanh), [dmt@ucsd.edu](mailto:dmt@ucsd.edu) (D.M. Tartakovsky), [scy@cbnu.ac.kr](mailto:scy@cbnu.ac.kr) (S.C. Yu).

Kouvel–Fisher (KF) [18], and the universal master curve [19] methods. A comparison of the critical exponents  $\beta$ ,  $\gamma$  and  $T_C$  obtained from the MAP and KF methods reveals that these values agree very well. Our analysis points to the coexistence of short- and long-range FM interactions in nanocrystalline  $\text{Fe}_2\text{Mn}_{1-x}\text{Cu}_x\text{Al}$ . Further, Cu doping in nanocrystalline  $\text{Fe}_2\text{Mn}_{1-x}\text{Cu}_x\text{Al}$  favors establishment of a long-range FM order.

## 2. Experiments

Nanocrystalline  $\text{Fe}_2\text{Mn}_{1-x}\text{Cu}_x\text{Al}$  ( $x=0.0, 0.1$  and  $0.3$ ) powders synthesized by means of high-energy ball milling technique, high-purity powder metals of Fe, Cu, Mn and Al (99.9%) were used as precursors. Stoichiometric ratios of the starting materials were mixed and milled for 96 h by a mechanical ball milling (SPEX 8000D with speed of 875 rpm). In this step, we used stainless-steel balls and vial. The starting materials were put in a vial (volume  $65\text{ cm}^3$ ), here the weighted ratio between balls and sample was about 8:1. The milling processes were carried out in an Argon atmosphere. After that, the room temperature crystal structure of the final products was checked by an X-ray diffractometer (Bruker AXS, D8 Discover) using a  $\text{Cu-K}\alpha$  radiation source. The magnetic measurements versus temperature and external magnetic field were performed on a vibrating sample magnetometer (VSM-Lakeshore 331).

## 3. Results and discussion

The X-ray diffraction (XRD) patterns of samples are shown in Fig. 1. It appears that the nanocrystalline  $\text{Fe}_2\text{Mn}_{1-x}\text{Cu}_x\text{Al}$  powders successfully prepared had a single phase. The Miller-indexed XRD peaks correspond to  $W$ -type structure disorder in full Heusler alloy belonging to the space group  $Im\bar{3}m$  [20]. By using the Scherrer–Debye formula,  $d=K\lambda/\beta_S \cos \theta$ , the average value of the nanocrystalline size ( $d$ ) can be obtained, where  $\beta_S$  is the full-width at half-maximum (FWHM) of an XRD peak,  $\theta$  is Bragg angle, and  $K=0.9$  is the shape factor. In this work, we used (1 1 1) XRD peak to estimate the values of  $d$  for samples. Thus, the values of  $d$  are found to be about 10 nm for all the samples.

In Fig. 2, it shows the temperature dependences of normalized magnetization  $M(T)/M_{\text{max}}$  for nanocrystalline  $\text{Fe}_2\text{Mn}_{1-x}\text{Cu}_x\text{Al}$  powders in an applied magnetic field of 100 Oe. One can see that with increasing temperature, all the samples reveal a steep FM–PM phase transition. Experimentally, it was found that this phase transition can be shifted to higher temperatures by increasing the Cu concentration. Here, the  $T_C$  values determined from the minimum of the  $dM/dT$  versus  $T$  curves are 406, 413 and 449 K for

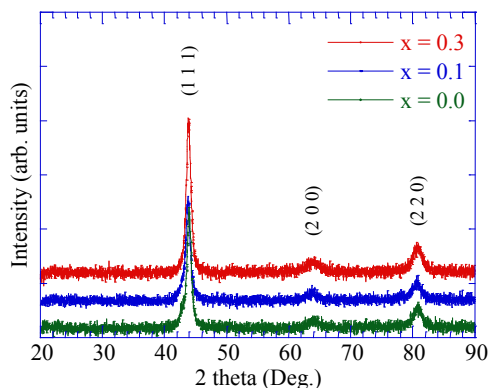


Fig. 1. XRD patterns for nanocrystalline  $\text{Fe}_2\text{Mn}_{1-x}\text{Cu}_x\text{Al}$  powders.

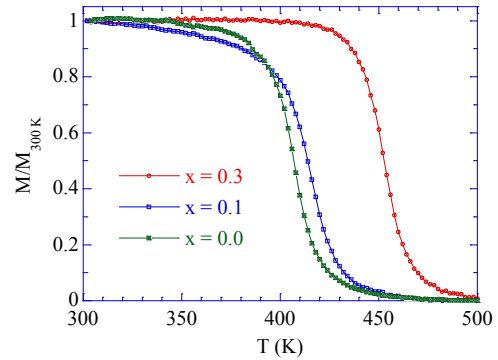


Fig. 2.  $M(T)/M_{300\text{ K}}$  curves for nanocrystalline  $\text{Fe}_2\text{Mn}_{1-x}\text{Cu}_x\text{Al}$  powders in the field  $H=100\text{ Oe}$ .

$x=0.0$ ,  $x=0.1$  and  $x=0.3$ , respectively.

To further understand the magnetic properties in the type of the phase-transition in the nanocrystalline  $\text{Fe}_2\text{Mn}_{1-x}\text{Cu}_x\text{Al}$  powders, we have studied their isothermal magnetization curves at various temperatures around  $T_C$ ,  $M(H, T)$ , see Fig. 3(a)–(c). One can see that the magnetization in the FM region does not reach saturation even at magnetic field up to 10 kOe. This feature can be due to the presence of magnetic disorder, magnetic inhomogeneity and/or anti-FM clusters in the samples. At a given  $H$ , the magnetization value decreases with increasing temperature. The FM nonlinear  $M(H)$  curves become linear when the sample enters the PM region. This magnetic phase separation can be seen more clearly if  $H/M$  is plotted versus  $M^2$  (corresponding to inverse Arrott plots of  $M^2$  versus  $H/M$ ) [21]. The nonlinear parts in the low-field region at temperatures below and above  $T_C$  are driven towards two opposite directions, see Fig. 3(d)–(f), revealing the FM–PM separation. According to Banerjee’s criteria [22], if some  $H/M$  versus  $M^2$  curves of a material show a negative slope, it exhibits the first-order phase transition (FOPT), while a positive slope corresponds to the second-order phase transition (SOPT). Comparing with these conditions reveals the FM–PM transitions of nanocrystalline  $\text{Fe}_2\text{Mn}_{1-x}\text{Cu}_x\text{Al}$  powders belonging to the SOPT, see Fig. 3(d)–(f).

According to the mean-field theory (MFT) proposed for a FM undergoing the SOPT and long-range FM interactions, the Landau free energy  $G_L$  is expanded in even powers of  $M$  [23]

$$G_L = aM^2 + bM^4 + \dots - HM \quad (1)$$

where  $a$  and  $b$  are temperature dependent parameters. By minimizing  $G_L$  ( $dG_L/dM=0$ ), we can obtain the relation

$$H/M = 2a + 4bM^2 \quad (2)$$

Eq. (2) implies that if magnetic interactions in a FM system exactly obey the MFT, the  $M^2$  versus  $H/M$  curves in the vicinity of  $T_C$  are straight lines. However, this feature is only observed in Fig. 3 (f), whereas it is not observed in Figs. 3(d) and 3(e). This result suggests an existence of short-range FM order in  $x=0.0$  and  $0.1$  samples, while a long-range FM order exists in  $x=0.3$  sample.

To determined the critical exponents ( $\beta$ ,  $\gamma$ , and  $\delta$ ) and  $T_C$  for nanocrystalline  $\text{Fe}_2\text{Mn}_{1-x}\text{Cu}_x\text{Al}$  samples, we tried to analyze the  $M(H)$  data according to the MAP method based on the Arrott–Noakes equation of state  $(H/M)^{1/\gamma} = a\varepsilon + bM^{1/\beta}$ , where  $\varepsilon=(T-T_C)/T_C$  is the reduce temperature [17]. This equation implies that with correct  $\beta$  and  $\gamma$  values the performance of  $M^{1/\beta}$  versus  $(H/M)^{1/\gamma}$  curves in the vicinity of  $T_C$  introduces parallel straight lines, and one of those lines passes through the coordinate origin at  $T_C$ . It is known that the SOPT near  $T_C$  is characterized by the critical exponents of  $\beta$  (associated with the spontaneous magnetization,  $M_S$ ),  $\gamma$  (associated with the initial magnetic susceptibility,  $\chi_0^{-1}$ ), and  $\delta$

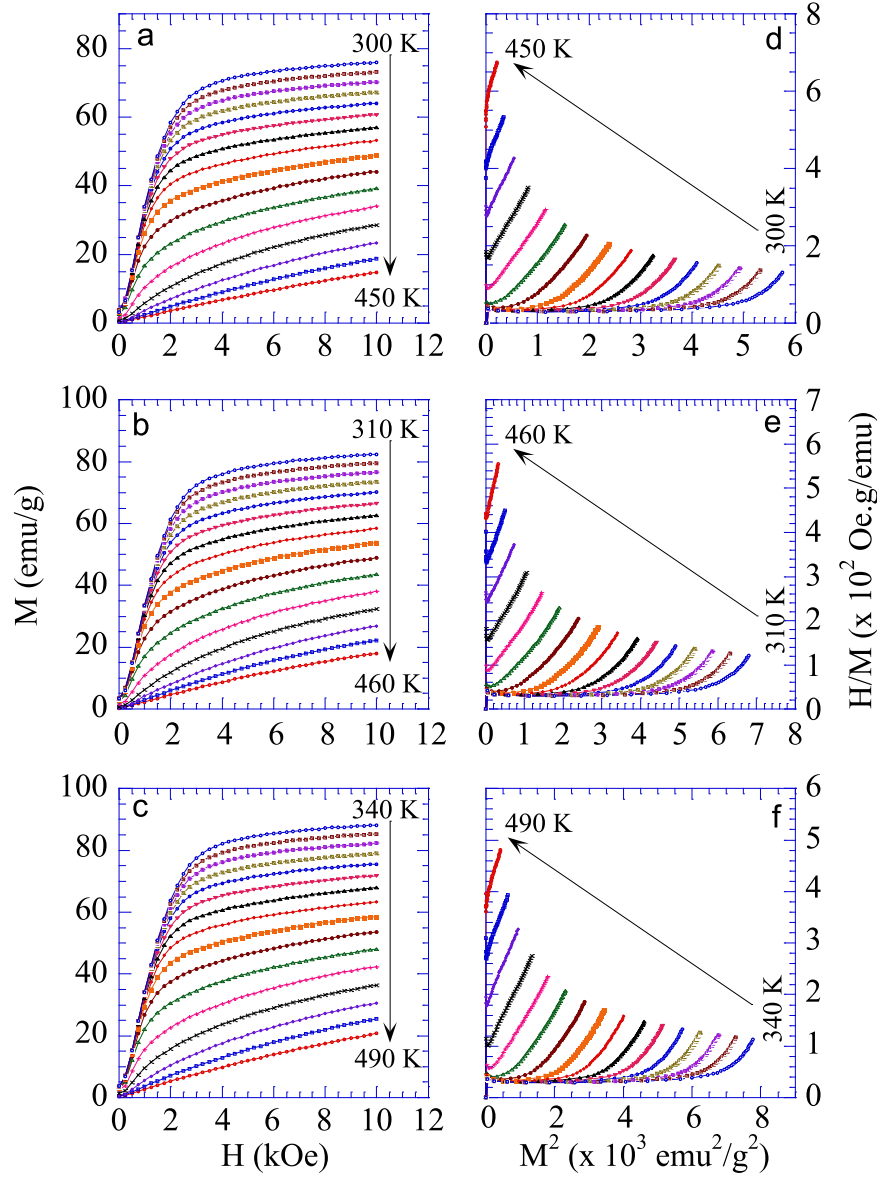


Fig. 3. (a)–(c)  $M(H)$  curves and (d)–(f)  $H/M$  versus  $M^2$  curves of nanocrystalline  $\text{Fe}_2\text{Mn}_{1-x}\text{Cu}_x\text{Al}$  powders, where  $x=0.0$  (a) and (d),  $x=0.1$  (b) and (e),  $x=0.3$  (c) and (f).

(associated with the critical isotherm). These parameters obey the following relations [21]:

$$M_S(T) = M_0(-\varepsilon)^\beta, \quad \varepsilon < 0 \quad (3)$$

$$\chi_0^{-1}(T) = (h_0/M_0)\varepsilon^\gamma, \quad \varepsilon > 0 \quad (4)$$

$$M = DH^{1/\delta}, \quad T = T_C \quad (5)$$

where  $M_0$ ,  $h_0/M_0$ , and  $D$  are the critical amplitudes. According to the MAP [17], values of  $M_S(T)$  and  $\chi_0^{-1}(T)$  are determined by plotting  $M^{1/\beta}$  versus  $(H/M)^{1/\gamma}$ . In our case, maybe the values of  $\beta$  and  $\gamma$  describing the nanocrystalline  $\text{Fe}_2\text{Mn}_{1-x}\text{Cu}_x\text{Al}$  samples will be different from those expected for the MFT (with  $\beta=0.5$  and  $\gamma=1.0$  [21]) because of the existence of short-range FM order in the samples with  $x=0.0$  and  $0.1$ , as mentioned above. The content of the MAP in determining accurate values of  $\beta$  and  $\gamma$  can be briefly described as follows. Starting from initial trial values of  $\beta=0.5$  and  $\gamma=1.0$ , the  $M_S(T)$  and  $\chi_0^{-1}(T)$  data obtained from the linear extrapolation are then fitted to Eqs. (3) and (4), respectively, to achieve better  $\beta$ ,  $\gamma$ , and  $T_C$  values. These new values are

continuously used for the next MAP to optimize their value. After iterating this process several times,  $\beta$ ,  $\gamma$ , and  $T_C$  converge to stable values.  $M_S(T)$  and  $\chi_0^{-1}(T)$  data fitted to Eqs. (3) and (4), respectively, with critical exponents obtained from the final step of MAP are shown in Fig. 4(a)–(c). This procedure gives accurate values of  $\beta$ ,  $\gamma$ , and  $T_C$  for samples as shown in Table 1. For the critical exponent of  $\delta$ , it can be obtained by using the Widom scaling relation [21]

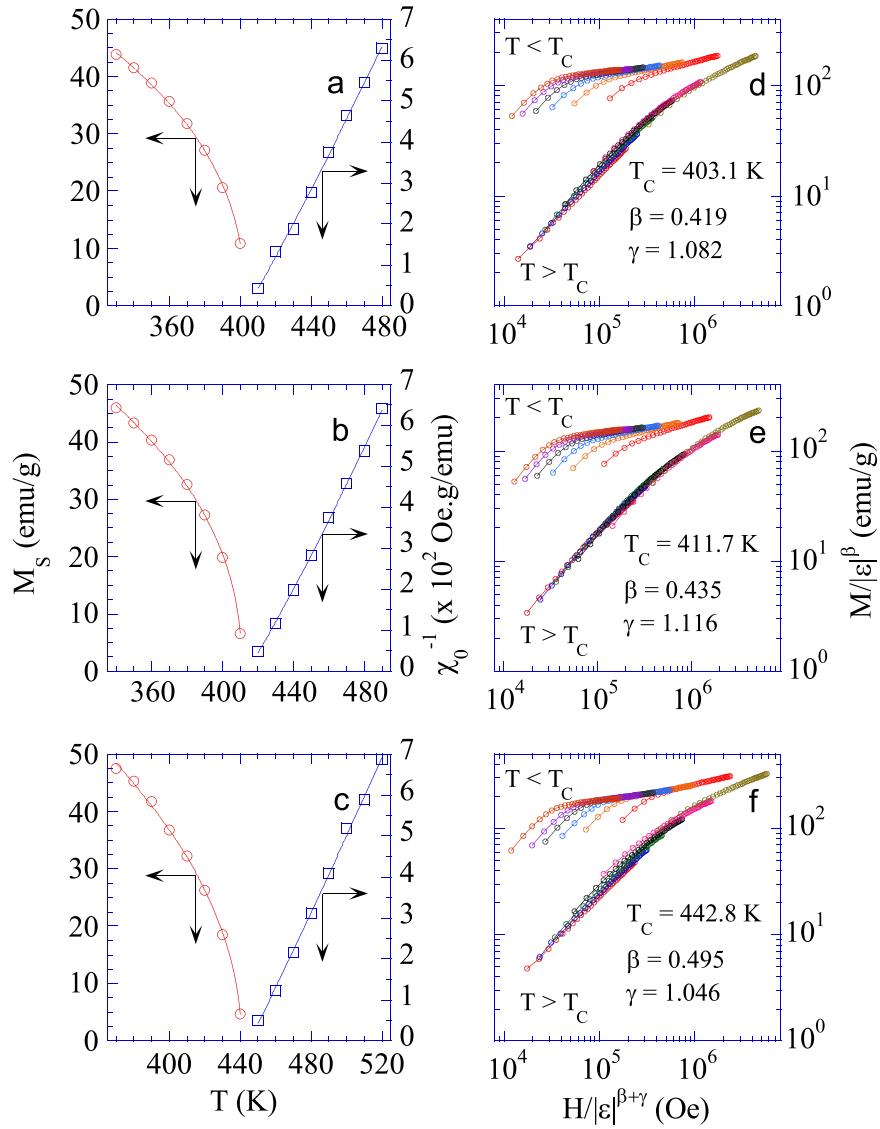
$$\delta = 1 + \gamma/\beta \quad (6)$$

From the values of  $\beta$  and  $\gamma$  for samples above obtained results, values of  $\delta$  are calculated to be 3.6, 3.6, and 3.1 for  $x=0.0, 0.1$ , and  $0.3$ , respectively.

The reliability of the obtained critical parameters can be verified by using the static-scaling theory, which predicts that the isothermal magnetization is a universal function of  $\varepsilon$  and  $H$  [21]:

$$M(H, \varepsilon) = \varepsilon^\beta f_\pm(H/|\varepsilon|^{\beta+\gamma}) \quad (7)$$

where  $f_+$  for  $T > T_C$  and  $f_-$  for  $T < T_C$  are regular functions. Eq. (7) implies that the behavior of the  $M/|\varepsilon|^\beta$  vs.  $H/|\varepsilon|^{\beta+\gamma}$  curves is such



**Fig. 4.** (a)–(c)  $M_S(T)$  and  $\chi_0^{-1}(T)$  curves, (d)–(f)  $M/|\epsilon|^\beta$  versus  $H/|\epsilon|^{\beta+\gamma}$  plots in the log–log scale for nanocrystalline  $\text{Fe}_2\text{Mn}_{1-x}\text{Cu}_x\text{Al}$  powders, where  $x=0.0$  (a) and (d),  $x=0.1$  (b) and (e),  $x=0.3$  (c) and (f).

**Table 1**  
The values of the critical exponents of nanocrystalline  $\text{Fe}_2\text{Mn}_{1-x}\text{Cu}_x\text{Al}$  powders compared with those of the theoretical models. Abbreviations: MAP: Modified Arrott plots; K–F: Kouvel–Fisher method.

Models/material	Method	$\beta$	$\gamma$	$\delta$	$T_C^a$ (K)	Ref.
Mean field theory		0.5	1.0	3.0	–	[21]
3D-Heisenberg model		0.365	1.336	4.7	–	[21]
3D-Ising model		0.325	1.241	4.8	–	[21]
Tricritical mean field theory		0.25	1.0	5.0	–	[24]
$x=0.0$	MAP	$0.419 \pm 0.012$	$1.082 \pm 0.051$	$3.6 \pm 0.1$	403.1	This work
	K–F	$0.414 \pm 0.011$	$1.011 \pm 0.041$	$3.4 \pm 0.1$	403.1	This work
$x=0.1$	MAP	$0.435 \pm 0.011$	$1.116 \pm 0.042$	$3.6 \pm 0.1$	411.7	This work
	K–F	$0.429 \pm 0.013$	$1.101 \pm 0.053$	$3.6 \pm 0.1$	411.0	This work
$x=0.3$	MAP	$0.495 \pm 0.015$	$1.046 \pm 0.035$	$3.1 \pm 0.1$	442.8	This work
	K–F	$0.487 \pm 0.015$	$1.077 \pm 0.046$	$3.2 \pm 0.1$	441.8	This work

<sup>a</sup> Values are obtained from critical behavior analyses.

that all  $M(H, T)$  data points fall on two universal branches characteristic of  $f_+$  for  $T > T_C$  and  $f_-$  for  $T < T_C$ . For our case, by plotting the  $M/|\epsilon|^\beta$  versus  $H/|\epsilon|^{\beta+\gamma}$  data on a log–log scale and using the critical exponents and the  $T_C$  obtained from the MAP

method, we can see that all the data fall onto two universal branches with  $T > T_C$  and  $T < T_C$ , see Fig. 4(d)–(f). This reflects that the critical parameters  $\beta$ ,  $\gamma$ , and  $T_C$  determined as described above are reliable. Notably, there is a small deviation of the  $M(H, T)$  data

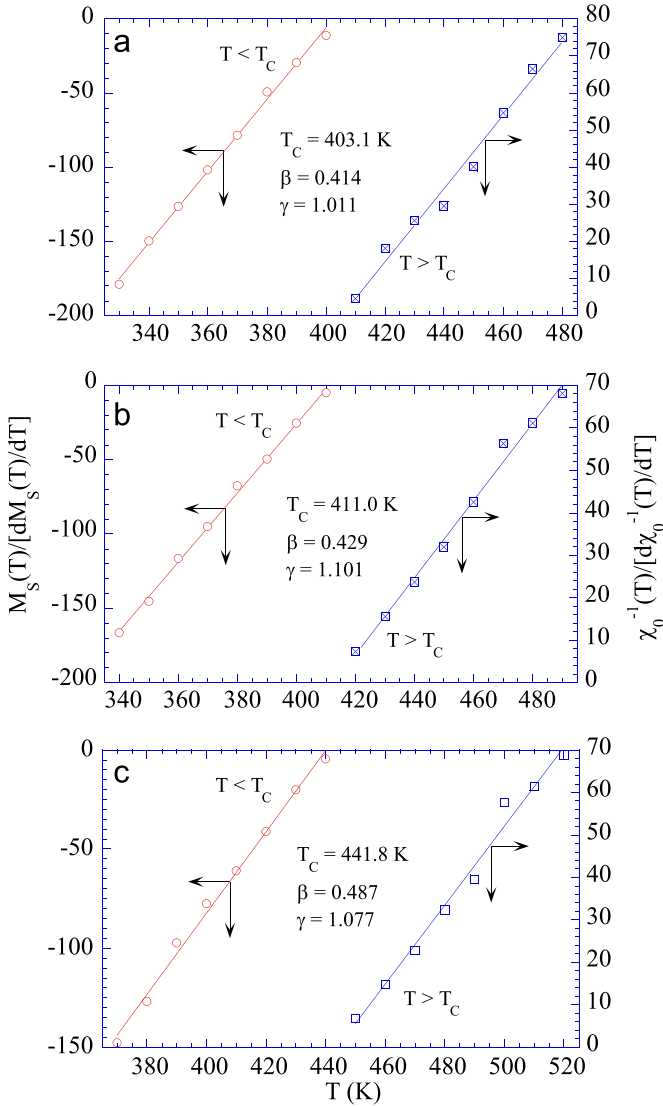


Fig. 5. Kouvel-Fisher plot of nanocrystalline  $\text{Fe}_2\text{Mn}_{1-x}\text{Cu}_x\text{Al}$  powders for (a)  $x=0.0$ , (b)  $x=0.1$  and (c)  $x=0.3$ .

from the universal curves in the  $M/|e|^\beta$  versus  $H/|e|^{\beta+\gamma}$  performance at low fields ( $H < 4$  kOe), which is related to the rearrangement of magnetic domains where magnetic moments are not completely aligned to the field.

Alternatively, the values of  $\beta$ ,  $\gamma$ , and  $T_C$  can be determined by the K-F method [18]. Using this method, the critical exponents  $\beta$  and  $\gamma$  could be independently determined. The K-F linear relations thus can be easily derived from Eqs. (3) and (4) as follows:

$$M_5(T) \left[ \frac{dM_5(T)}{dT} \right]^{-1} = (T - T_C) / \beta \quad (8)$$

$$\chi_0^{-1}(T) \left[ \frac{d\chi_0^{-1}(T)}{dT} \right]^{-1} = (T - T_C) / \gamma \quad (9)$$

The K-F method consists of an iterative procedure, which starts by constructing the Arrott-Noakes plot (i.e., the plot of  $M^{2.5}$  versus  $(H/M)^{0.75}$  [17]). According to the K-F method, plots of  $M_5(dM_5/dT)^{-1}$  versus  $T$  and  $\chi_0^{-1}(d\chi_0^{-1}/dT)^{-1}$  versus  $T$  should yield straight lines with slopes  $1/\beta$  and  $1/\gamma$ , respectively. By the extrapolation, these straight lines give intercepts on the  $T$  axis equal to the  $T_C$ . Detailed descriptions of the K-F method can be found elsewhere [18]. The K-F plots of the final results for

nanocrystalline  $\text{Fe}_2\text{Mn}_{1-x}\text{Cu}_x\text{Al}$  samples are shown in Fig. 5(a)–(c). The values of  $\beta$ ,  $\gamma$ , and  $T_C$  for samples obtained from final step of K-F method are shown in Table 1. Using these  $\beta$  and  $\gamma$  values, the values of  $\delta$  are found to be 3.4, 3.6, and 3.2 for  $x=0.0$ , 0.1, and 0.3, respectively, calculated from the Widom scaling relation, Eq. (6) [21]. One can see that the critical parameters obtained from both the MAP and the K-F methods match well. This reflects that the values of  $\beta$ ,  $\gamma$ , and  $T_C$  determined as described above are reliable.

Comparing the values of the critical exponents obtained for nanocrystalline  $\text{Fe}_2\text{Mn}_{1-x}\text{Cu}_x\text{Al}$  samples and of the theoretical models [21;24] is shown in Table 1. Clearly, the values  $\beta=0.419$  and  $0.435$ ,  $\gamma=1.082$  and  $1.116$  obtained by the MAP method and  $\beta=0.414$  and  $0.429$ ,  $\gamma=1.011$  and  $1.101$  obtained by the K-F method for  $x=0.0$  and  $0.1$ , respectively, are located between those of the MFT and the 3D-Heisenberg model. Whereas, the values  $\beta=0.495$  and  $\gamma=1.046$  obtained by the MAP method and  $\beta=0.487$  and  $\gamma=1.077$  obtained by K-F method for  $x=0.3$  are more close to those expected for the MFT. However, the  $\beta$  values obtained are lower than  $\beta=0.5$ . These results suggest a coexistence of the short- and long-range FM interactions in these samples. Among these, long-range FM interaction could be associated with the core of nanocrystals. In contrast, short-range FM interaction corresponding to magnetic inhomogeneities in the samples are thought to surface-related effects, lattice strain and distortions, which lead to the weakening of the FM interaction strength. Notably, the  $\beta$  values obtained for Cu-doped samples shift towards that expected for the MFT. It means that Cu-doping into nanocrystalline  $\text{Fe}_2\text{Mn}_{1-x}\text{Cu}_x\text{Al}$  tends to result in long-range FM order. In other words, the samples become more magnetically homogeneous with increasing Cu-doping.

To get more information on critical properties of nanocrystalline  $\text{Fe}_2\text{Mn}_{1-x}\text{Cu}_x\text{Al}$  powders, we have also investigated the MCE of the samples via magnetic entropy change ( $\Delta S_m$ ) based on  $M(H, T)$  data in vicinity of  $T_C$  shown in Figs. 3(a)–(c). It is known that the MCE is an intrinsic property and response of magnetic materials with respect to the application or removal of magnetic field, which is maximized near  $T_C$ . According to the thermodynamic theory,  $\Delta S_m$  produced by the variation of a magnetic field variation from 0 to  $H$  is expressed by [21]

$$\Delta S_m(T, H) = \int_0^H \left( \frac{\partial M}{\partial T} \right)_H dH \quad (10)$$

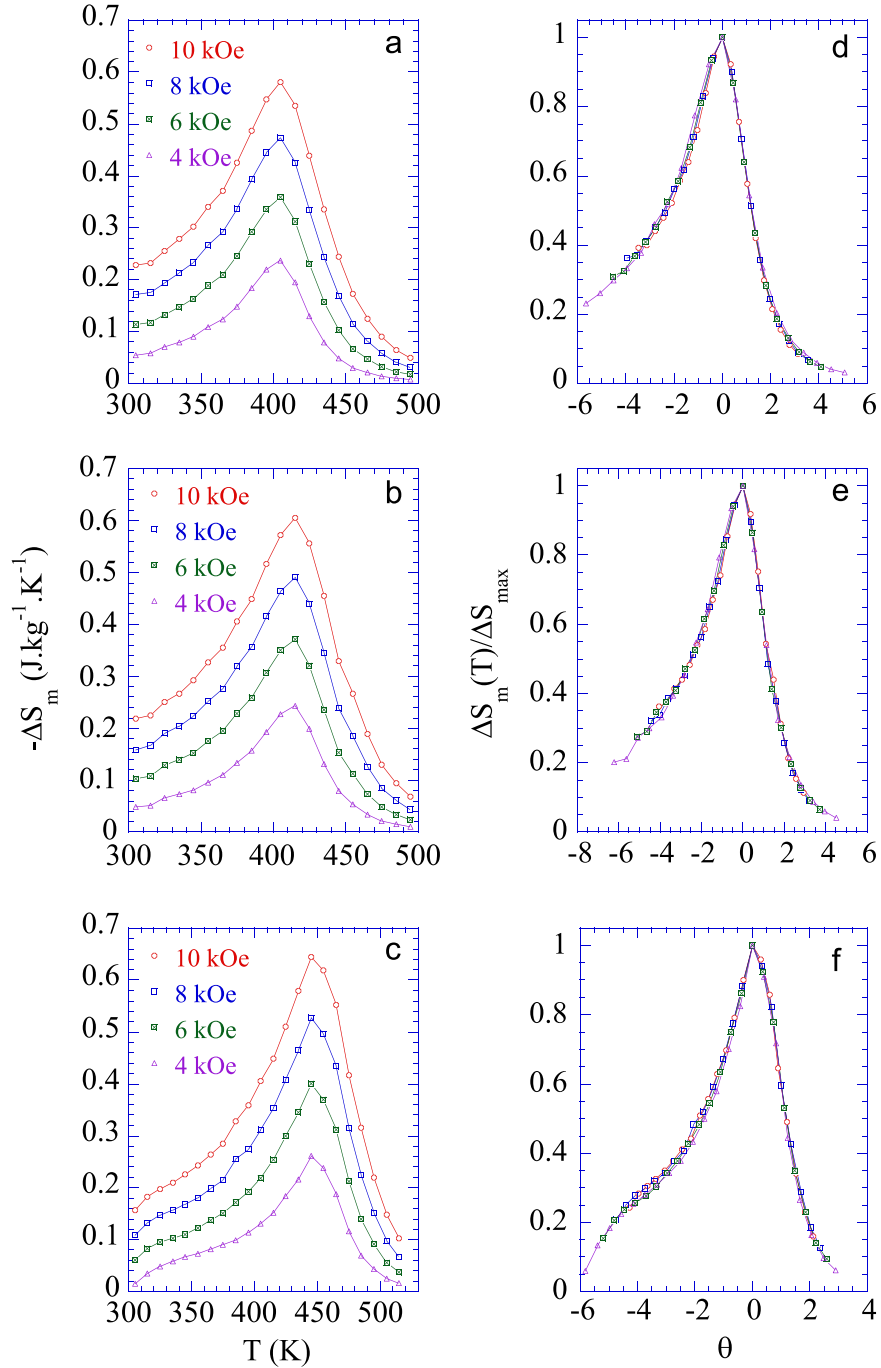
Fig. 6(a)–(c) show  $-\Delta S_m(T)$  curves of the samples under applied magnetic field changes  $H=4-10$  kOe (with step of 2 kOe). For each sample at a given temperature,  $|\Delta S_m|$  increase with increasing  $H$ . As a function of temperature,  $-\Delta S_m(T)$  curve reaches a maximum value around  $T_C$ . With  $H=10$  kOe,  $|\Delta S_{\max}|$  values of the samples are 0.58, 0.61, and 0.65  $\text{J kg}^{-1} \text{K}^{-1}$  for  $x=0.0$ , 0.1, and 0.3, respectively.

Recently, a new method to describe  $T$  and  $H$  dependences of  $\Delta S_m$ ,  $\Delta S_m(T, H)$ , for SOPT materials has been introduced Franco and Conde [19]. According to this method, all  $\Delta S_m(T)$  curves measured at different  $H$  values will collapse into a universal curve when  $\Delta S_m(T)$  curves are normalized to their respective peak value (i.e.,  $\Delta S_m(T)/\Delta S_{\max}$ ), and the temperature axis above and below  $T_C$  is rescaled as

$$\theta = (T - T_C) / (T_r - T_C) \quad (11)$$

where  $T_r$  is the reference temperature corresponding to a certain fraction  $k$  that fulfils  $\Delta S_m(T_r)/\Delta S_{\max}=k$ . The choice of  $k$  does not affect the actual construction of the universal curve. In this work, we identified  $T_C$  as the temperature at the peak of the  $-\Delta S_m(T)$  curve, and selected  $k=0.6$  when constructing the universal curve for each sample. It means that  $T_r$  values are selected at  $\Delta S_m(T_r)/\Delta S_{\max}=0.6$  to rescale the temperature axis. Fig. 6(d)–





**Fig. 6.** (a)–(c)  $-\Delta S_m(T)$  curves at different fields ranging from 4 to 10 kOe with step 2 kOe, (d)–(f) universal master curves for nanocrystalline  $\text{Fe}_2\text{Mn}_{1-x}\text{Cu}_x\text{Al}$  powders, where  $x=0.0$  (a) and (d),  $x=0.1$  (b) and (e),  $x=0.3$  (c) and (f).

(f) shows the universal master curves for nanocrystalline  $\text{Fe}_2\text{Mn}_{1-x}\text{Cu}_x\text{Al}$  powders measured at different  $H=4\text{--}10$  kOe. Clearly, the overlap of the different curves is reasonable in the whole temperature range. It means that the  $\Delta S_m(T, H)$  data for nanocrystalline  $\text{Fe}_2\text{Mn}_{1-x}\text{Cu}_x\text{Al}$  powders follow a universal curve for magnetic entropy change. This is a familiar character of the SOPT material [25]. The overlap of  $\Delta S_m(T, H)$  data into a unique curve is an additional confirmation of the general validity of the treatment in SOPT materials.

#### 4. Conclusion

Critical properties of nanocrystalline  $\text{Fe}_2\text{Mn}_{1-x}\text{Cu}_x\text{Al}$  powders

with  $x=0, 0.1$ , and  $0.3$  prepared by the high energy ball milling technique were investigated in detailed. Our experimental results demonstrated the FM–PM phase transition in the samples to be SOPT with critical exponents  $\beta=0.419\text{--}0.495$ ,  $\gamma=1.046\text{--}1.116$  obtained by MAP method and  $\beta=0.414\text{--}0.487$ ,  $\gamma=1.011\text{--}1.101$  obtained by K–F method. These values are not belonging to any universality class. They are located between those of the MFT and the 3D–Heisenberg model suggesting a coexistence of short- and long-range FM order in the samples. The samples become more magnetically homogeneous with increasing Cu-doping. Additionally, the  $\Delta S_m(T)$  data measured at different applied magnetic field changes are collapsed into a universal master curve by normalizing  $\Delta S_m(T)/\Delta S_{m,\text{max}}$  versus  $\theta=(T-T_C)/(T_1-T_C)$ . The follow a

universal curve of  $\Delta S_m(T, H)$  data is an additional confirmation the the FM–PM transitions of nanocrystalline  $\text{Fe}_2\text{Mn}_{1-x}\text{Cu}_x\text{Al}$  powders belonging to the SOPT.

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