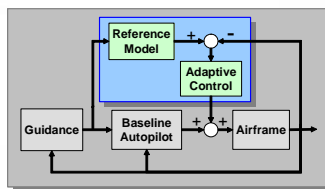




Cooperative Control Challenges for Aerial Vehicles



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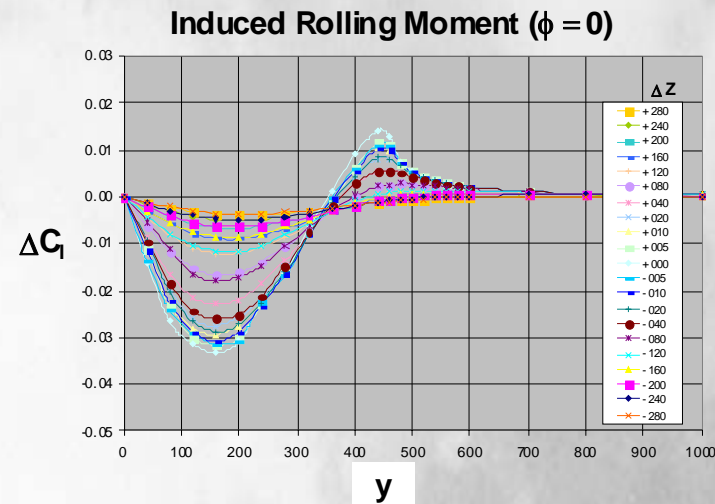
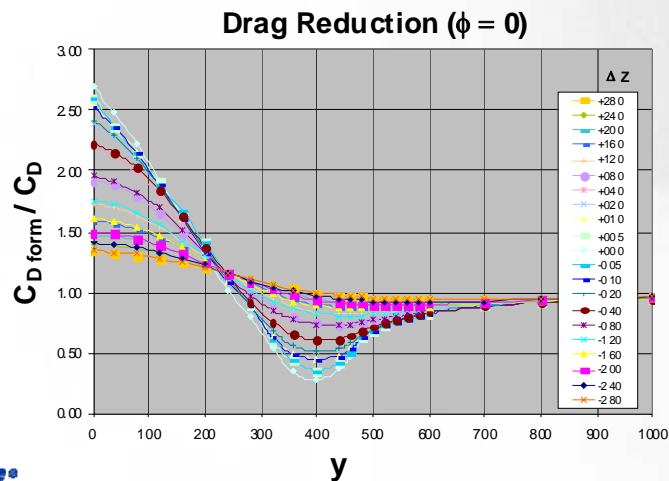
Presentation Overview

- **Introduction**
 - **Single vehicle → Multiple Vehicles → Waves of multiple vehicles**
- **Control Challenge Problems**
 - **Single Vehicle in Close-Coupled Flight with a Leader**
 - ✓ Simplified Flight Dynamics
 - ✓ Applications
 - Autonomous Aerial Refueling, (AAR)
 - Autonomous Formation Flight, (AFF)
 - **Multiple Unmanned Aerial Vehicles, (UAVs)**
 - ✓ Simplified UAV dynamics
 - Dubins' car
 - Dubins' aircraft
 - ✓ Collaborative Control in Hostile / Adversarial Environment
 - Task allocation
 - Path planning
 - Cooperative attack
 - Intelligence Surveillance and Reconnaissance, (ISR)
 - **“Ultimate” Challenge**
 - ✓ Waves of multiple UAVs prosecuting multiple targets in uncertain environment
- **Conclusions**

Close-Coupled Flight Dynamics and Control

- **Aerodynamic Phenomenon**

- Unknown unsteady flow field behind lead aircraft
- Lead aircraft wingtip vortices influence trailing aircraft aerodynamic forces and moments
 - ✓ **Longitudinal separation**
 - changes are uniform within 5 aircraft body length
 - ✓ **Vertical and Lateral Separation**
 - induced aerodynamic drag
 - rolling moment
 - ✓ **Relative bank angle**



Close-Coupled Flight: System Dynamics

- Trailing aircraft in close-coupled formation (relative dynamics)

- 2 Control Inputs

- Thrust for Airspeed
 - Differential Aileron for Roll

- Unknown Constant Parameters

- Throttle effectiveness
 - Roll damping
 - Aileron effectiveness

- Unknown functions

- Vortex induced aerodynamics
 - Drag force $D(y, \varphi)$
 - Rolling moment $\Delta L(y, \varphi)$

- Applications

- Autonomous Formation Flight
 - Autonomous Aerial Refueling

$$\dot{d} = V \left[\begin{array}{l} \text{airspeed} \\ \text{Thrust} \end{array} \right]$$

$$\dot{V} = T_{\delta_T} \delta_T - D(y, \varphi) \left[\begin{array}{l} \text{induced drag force} \end{array} \right]$$

$$\ddot{y} = g n_z \varphi \left[\begin{array}{l} \text{bank angle} \end{array} \right]$$

$$\dot{\varphi} = p \left[\begin{array}{l} \text{roll rate} \\ \text{Diff Aileron} \\ \text{induced rolling moment} \end{array} \right]$$

$$\dot{p} = L_p p + L_{\delta_a} \delta_a + \Delta L(y, \varphi)$$

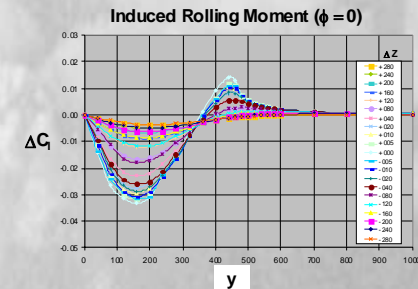
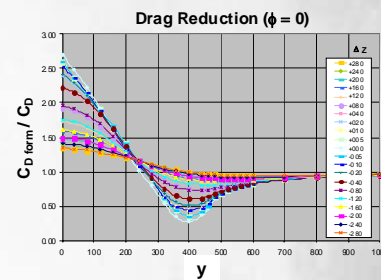


Autonomous Aerial Refueling, (AAR)



Autonomous Formation Flight, (AFF)

$$\begin{aligned} D(-y, \varphi) &= D(y, \varphi) \\ \Delta L(-y, \varphi) &= -\Delta L(y, \varphi) \end{aligned}$$

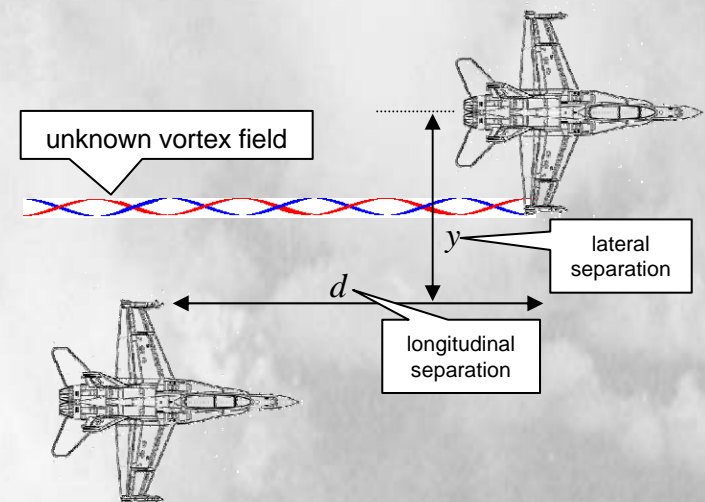
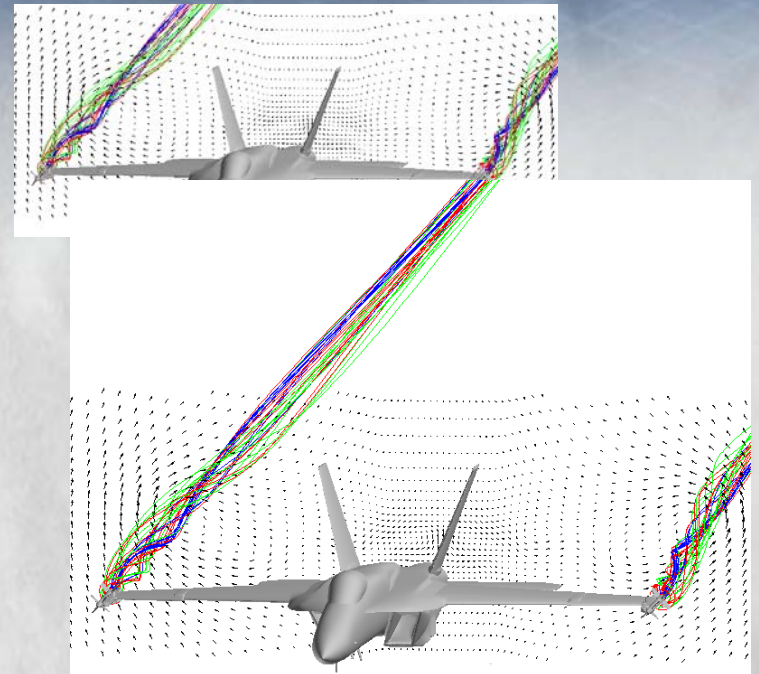


Close-Coupled Flight: AFF Control Challenge

- **Benefit**
 - Flying in the vortex field
 - ✓ reduces induced drag by 20 - 25%
 - range extension
 - less fuel
- **Control Challenges**
 - wingtip vortex induced uncertainties
 - unknown / unsteady vortex location
- **Control Goals**
 - Bounded tracking
 - Vortex seeking → drag reduction



F/A-18 Formation Flight Tests @ NASA Dryden, 2000

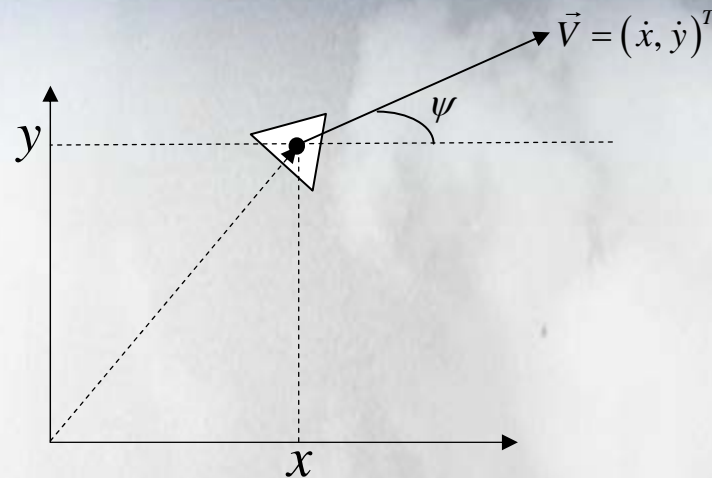


UAV Dynamics for Control Design

- **Dubins' Car**

$$\begin{aligned} \dot{x} &= V \cos \psi \\ \dot{y} &= V \sin \psi \\ \dot{\psi} &= \dot{\psi}_{\max} u_{\psi} \\ \dot{V} &= \dot{V}_{\max} u_V \end{aligned}$$

turn control
max turn rate
speed control
max thrust



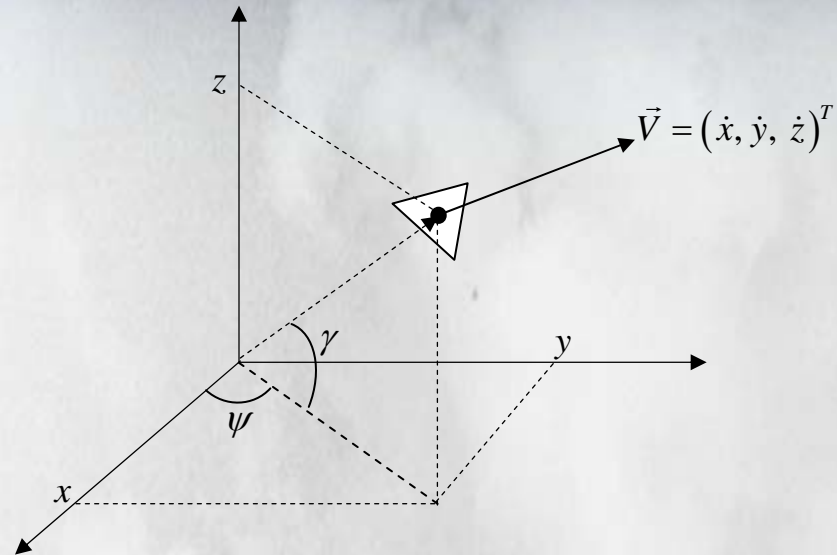
- **2 control inputs**
 - ✓ Speed control, (thrust)
 - limited between 0 and 1
 - ✓ Heading control, (rate of turning)
 - limited between 0 and 1
- **2 controlled outputs**
 - ✓ (x, y) - positions

UAV Dynamics for Control Design (continued)

- **Dubins' Aircraft**

$$\begin{aligned} \dot{x} &= V \cos \gamma \cos \psi \\ \dot{y} &= V \cos \gamma \sin \psi \\ \dot{z} &= V \sin \gamma \\ \dot{\gamma} &= \dot{\gamma}_{\max} u_{\gamma} \\ \dot{\psi} &= \dot{\psi}_{\max} u_{\psi} \\ \dot{V} &= \dot{V}_{\max} u_V \end{aligned}$$

climb control
max climb rate
turn control
max turn rate
speed control
max thrust



- **3 control inputs**

- ✓ Speed control, (thrust)
 - limited between 0 and max thrust available
 - ✓ Heading and flight path controls, (turn and climb rates)
 - limited between 0 and 1

- **3 controlled outputs**

- ✓ (x, y, z) - positions

Control Challenge: Single UAV Path Planning

- **Single vehicle operating in uncertain environment**

- Finding “shortest” path in finite graph

- ✓ System dynamics

- Simple model: $x_{k+1} = u_k$
- Dubins' car / aircraft model
- Other

$$\begin{aligned}\dot{x} &= V \cos \psi \\ \dot{y} &= V \sin \psi \\ \dot{\psi} &= \dot{\psi}_{\max} u_{\psi} \\ \dot{V} &= \dot{V}_{\max} u_V\end{aligned}$$

$$\begin{aligned}\dot{x} &= V \cos \gamma \cos \psi \\ \dot{y} &= V \cos \gamma \sin \psi \\ \dot{z} &= V \sin \gamma \\ \dot{\gamma} &= \dot{\gamma}_{\max} u_{\gamma} \\ \dot{\psi} &= \dot{\psi}_{\max} u_{\psi} \\ \dot{V} &= \dot{V}_{\max} u_V\end{aligned}$$

- Optimality criterion

- ✓ not a distance-like measure
 - doesn't satisfy the triangular inequality
- ✓ instant connection cost matrix is not-symmetric

- “Optimal” path / route

- node precedence constraints
- obstacles and pop-up threats avoidance
- collision avoidance with other vehicles

Constrained Shortest Path Problem

Control Challenge: Task Allocation

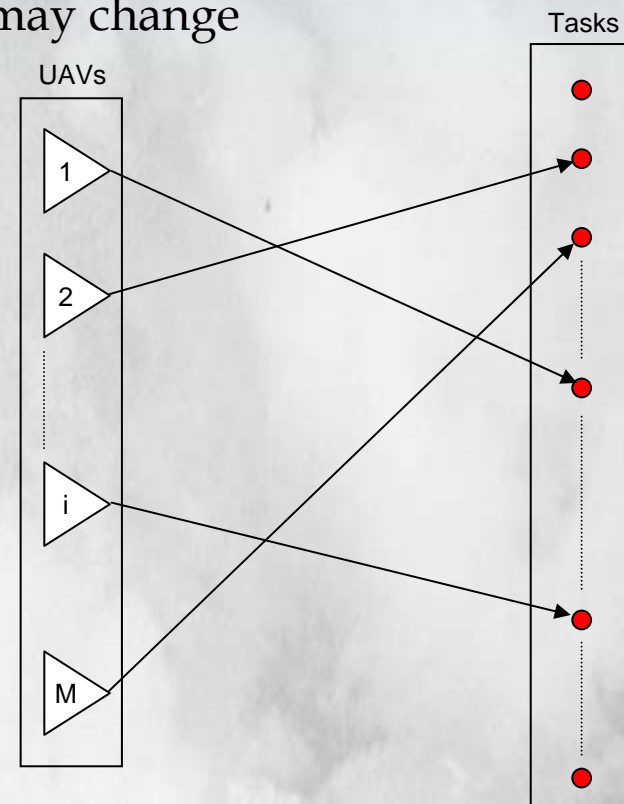
- **Dynamic Optimization Problem**

- M vehicles \rightarrow N Tasks, ($M < N$)
 - ✓ number of assets (M) and tasks (N) may change

- **Goal**

- ✓ maximize total assignment benefit
- ✓ account for vehicle capabilities

- Online solution computation



Constrained Optimal Assignment Problem

Control Challenge: Cooperative Attack

- **Multiple UAVs Prosecuting Multiple Targets**
 - **Task allocation**
 - ✓ Constraints
 - individual vehicle capability
 - time-critical targets
 - task precedence
 - relative timing
 - **Path / Route planning**
 - ✓ Obstacle & Collision Avoidance
 - **Sensing, Estimation and Information Sharing**
 - ✓ Uncertain & hostile environment
 - ✓ Limited communication data links

Constrained Multi-Vehicle Shortest Path and Travelling Salesman Problems

“Ultimate” Challenge

- **Single UAV → Multiple UAVs → Waves of Multiple UAVs**
 - Performing tasks to accomplish higher level objectives
- **Collaborative Control Tasks in Uncertain Environment**
 - Cooperative Strike, Intelligence Surveillance Reconnaissance (ISR)
 - Task allocation, Route planning, and Obstacle Avoidance
 - Task precedence and timing constraints
 - ✓ Prosecution of time critical targets
 - Execution in the presence of uncertainty caused by adversarial actions
 - ✓ threat location, anti-tactics
 - ✓ degraded communications
- **Information Management Between Platforms**
 - Support data fusion / estimation and collaboration
 - ✓ limited available data links
 - ✓ interruptions of service
 - ✓ degraded performance

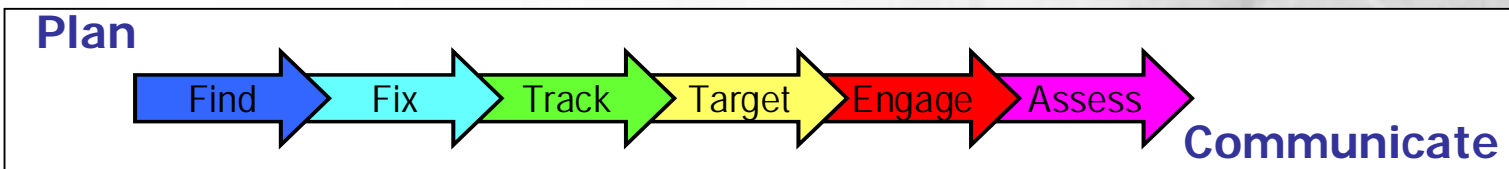
Conclusions

- **Control Challenge Problems for Aerial Vehicles**

- single UAV
- multiple UAVs
- waves of multiple UAVs

- **Need Close-to-Real-Time Control Solutions**

- Frequently generate “optimal” task assignment and multi-vehicle routes in the presence of:
 - ✓ uncertain and hostile environment
 - ✓ battle damage
 - ✓ limited communications
- Assign and prosecute time-critical targets



Shorten the Kill Chain

