# Data based modeling and control of a dual-stage actuator hard disk drive

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Abstract—A data-based approach is presented for modeling and controller design of a dual-stage servo actuator in a hard disk drive. The servo actuator in this hard disk drive consists of a conventional voice coil motor and a piezo-electrically actuated suspension. A weighted Hankel matrix based realization algorithm that uses frequency domain data is applied to estimate a discrete-time model of the voice coil motor and the piezoelectric actuator. Based on the discrete-time models, different dual-stage track-following controllers were designed using classic and  $H_{\infty}$  loop shaping techniques. The controllers were implemented in real-time in the investigated hard disk drive. A stable feedback control and good agreement between measurement and simulated results show the promising result of data based modeling and control.

# I. INTRODUCTION

Hard disk drives have improved enormously in terms of storage capacity, data access time and miniaturization over the last couple of decades, although their main functional principle has not changed substantially. Figure 1 shows a commercially available hard disk drive that contains a dualstage actuated suspension. Dual-stage actuation is believed to be a solution in order to meet the higher accuracy and speed requirements on the servo mechanism as storage density increases [1]. A number of different approaches for a second



Fig. 1. Schematic of the investigated dual-stage actuated hard disk drive.

stage actuator in a hard disk drive (HDD) servo system have been explored based on either electrostatic/electromagnetic

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effects ([2]-[9]) or on piezoelectric principles ([10]-[12]). The actuators are either mounted on the suspension or on the slider. The dual-stage hard disk drive considered in this paper uses a actuator based on a piezoelectric transducer (PZT). The magnified portion of Fig. 1 shows a micro-actuator mounted on a suspension. The micro-actuator has a limited stroke, and, thus, it is more useful for track-following than for track-seeking [13]. A close-up of the slider with the suspension and the PZT elements is shown in Fig.2. This paper shows frequency domain based modeling and



Fig. 2. Piezo-electric push/pull actuated suspension in a commercial available hard disk drive.

control design of a dual-stage actuator in a hard drive. Known dual-stage control design techniques such as the sensitivity decoupling method (SDM) [1], [3] and an  $H_{\infty}$  loop shaping algorithm are applied [21].

#### II. MODELING AND SYSTEM IDENTIFICATION

In order to be able to inject control signals, the hard disk drive servo controller is bypassed completely. The circuit board was disconnected from the HDD and all motor drivers were replaced. Since the position error signal (PES) of the servo mechanism is not directly available, a laser Doppler vibrometer (LDV) is used to measure the radial slider motion. To accomplish visual access to the slider the HDD must be modified. The top cover was replaced with one made out of plexiglas and a mirror was used to deflect the laser beam onto the side of the slider. The experimental set-up illustrated in Fig. 3 was used to determine the frequency response function of both actuators.

The estimation of a discrete-time model is based on the eigensystem realization algorithm [14] but uses frequency domain data that is converted into time domain data first. Additional frequency-dependent weighting functions are used to emphasize control relevant resonance modes of the actuator response. The inverse discrete Fourier transform (IDFT) of the frequency response function (FRF) measurement yields an estimate for the impulse response of the system. The impulse response coefficients (Markov parameters) are defined



Fig. 3. Schematic of the experimental set-up to determine the frequency response function of the dual-stage actuator.

by

$$g_k = \frac{1}{2N} \sum_{l=0}^{2N-1} G_l e^{j\omega_k l}, \quad k = 0, 1, \cdots, 2N - 1$$
 (1)

where  $G_l$  contains the FRF data and  $\omega_k$  is the frequency vector defined by

$$\omega_k = \frac{\pi k}{N}, \quad k = 0, 1, \cdots, 2N - 1$$
 (2)

N denotes the number of FFT lines (frequency points) in the FRF measurements. The measured data are stored in a Hankel matrix **H** that contains the Markov parameter estimates defined in (1). By choosing m as the number of impulse response samples taken into account, one can define a  $m \times m$  Hankel matrix by

$$\mathbf{H} = \begin{bmatrix} g_1 & g_2 & \cdots & g_m \\ g_2 & g_3 & \cdots & g_{m+1} \\ \vdots & \vdots & \vdots & \vdots \\ g_m & g_{m+1} & \cdots & g_{2m-1} \end{bmatrix}$$
(3)

The shifted version  $\mathbf{\bar{H}}$  is defined by

$$\bar{\mathbf{H}} = \begin{bmatrix} g_2 & g_3 & \cdots & g_{m+1} \\ g_3 & g_4 & \cdots & g_{m+2} \\ \vdots & \vdots & \vdots & \vdots \\ g_{m+1} & g_{m+2} & \cdots & g_{2m} \end{bmatrix}$$
(4)

To perform a control orientated modeling by means of capturing relevant resonance modes only, an input weighting filter  $F_u$  is used. Performing an IDFT on  $F_u$  yields

$$g_{u_k} = \frac{1}{2N} \sum_{l=0}^{2N-1} F_{u_k} e^{j\omega_k l}, k = 0, 1, \cdots, 2N - 1 \quad (5)$$

The impulse response of the weighting filter  $g_{u_k}$  is stored in a  $N \times N$  Toeplitz matrix defined by

$$\mathbf{\Gamma}_{\mathbf{u}} = \begin{bmatrix} g_{u_0} & g_{u_1} & \cdots & g_{u_{N-1}} \\ 0 & g_{u_0} & \cdots & g_{u_{N-2}} \\ \vdots & \vdots & \vdots & \vdots \\ 0 & 0 & \cdots & g_{u_0} \end{bmatrix}$$
(6)

The procedure used in this paper has been previously reported in [15] and [16]. The singular value decomposition (SVD) is applied to the weighted Hankel matrix  $H_w$  defined by

$$\mathbf{H}_{\mathbf{w}} = \mathbf{H} \boldsymbol{\Gamma}_{\mathbf{u}} = \mathbf{U} \boldsymbol{\Sigma} \mathbf{V}^{\mathrm{T}}$$
(7)

where V, U and  $\Sigma$  represent the unitary matrices and the singular value matrix of a standard SVD. The SVD is used to reduce  $\mathbf{H}_{\mathbf{w}}$  to a matrix with rank n

$$\mathbf{H}_{\mathbf{w}\,\mathbf{n}} = \mathbf{H}_{\mathbf{1}}\mathbf{H}_{\mathbf{2}} \tag{8}$$

where  $H_1$  and  $H_2$  are defined by

$$\mathbf{H}_{1} = \mathbf{U}_{n} \boldsymbol{\Sigma}_{n}^{1/2}, \quad \mathbf{H}_{2} = \boldsymbol{\Sigma}_{n}^{1/2} \mathbf{V}_{n}^{\mathrm{T}}$$
(9)

An estimation for the state space matrix  $\mathbf{A}$  is

$$\mathbf{A} = \mathbf{H}_1^* \bar{\mathbf{H}_w} \mathbf{H}_2^* \tag{10}$$

where  $\mathbf{H}_{1}^{*}$  and  $\mathbf{H}_{2}^{*}$  denote the left and right inverse of  $\mathbf{H}_{1}$ and  $\mathbf{H}_{2}$ , respectively. The input matrix **B** becomes the first column of  $\mathbf{H}_{2}\Gamma_{u}^{-1}$ . The first row of  $\mathbf{H}_{1}$  forms the output matrix **C**. The feed-through term **D** is estimated solving a least squares optimization [15]. For the VCM modeling, first an estimated second order model  $G_{2nd}$  representing the main actuator dynamics including the low frequency friction mode at 17 Hz is removed from the FRF measurement and added back to the model after the estimation. The second order model (here given in continuous time) is parameterized by

$$G_{2nd} = \frac{K_v \omega_0^2}{s^2 + 2\delta\omega_0 s + \omega_0^2}$$
(11)

and the parameters are given by  $K_v = 9750$ ,  $\omega_0 = 17 \cdot 2\pi \frac{\text{rad}}{\text{s}}$ ,  $\delta = 0.2$ . The measurements and the estimated models of both actuators are depicted in Fig. 4 and Fig. 5, respectively. The figures show the Bode diagram from voltage input in Volts to head displacement in  $\mu$ m.

# **III. CONTROLLER DESIGN**

#### A. General overview

One of the main characteristics of a dual-stage controller in HDDs is that there are two control outputs but there is only one position feedback signal available that includes the contribution of both actuators. The relative displacement between the two actuators is not measured in an actual disk drive. Several different control design techniques for dual-stage actuators have been developed in recent years [3],[23]. One of them is the PQ method [17] that is based on loop shaping. It is shown in [17] that by placing the closed-loop zeros of the feedback connection of plant Pand compensator Q one can achieve frequency separation



Fig. 4. Comparison of FRF measurement and estimated 15th order VCM model



Fig. 5. Comparison of FRF measurement and estimated 20th order PZT model

between both actuators. Here, P is defined as the ratio of the VCM and the PZT model and the compensator Q is defined in the same manner. Application examples of the PQ method are given in [16] and [18]. In this study, P yields a non-minimum phase system which limits bandwidth and makes it much more difficult to perform loop shaping based control design. Instead, we applied the sensitivity decoupling method (SDM) as a classical control design technique and an  $H_{\infty}$ -based optimal control algorithm. Both design methods will be explained briefly in the next two subsections.

# B. Sensitivity decoupling method

The sensitivity decoupling method (SDM) [1], [3] allows a separate controller design for the VCM and the PZT. The control structure is given in Fig. 6. The displacement of the PZT is estimated using a simplified PZT model  $\hat{G}_{PZT}$ . From Fig. 6, we extract the sensitivity function  $S_T = \frac{y}{d}$  of the



Fig. 6. Control structure of sensitivity decoupling method

overall system

$$S_T = \underbrace{\frac{1}{1 + C_{PZT}G_{PZT}}}_{S_{PZT}} \cdot \underbrace{\frac{1}{1 + K \cdot C_{VCM}G_{VCM}}}_{S_{VCM}}$$
(12)

where  $G_{(VCM,PZT)}$  and  $C_{(VCM,PZT)}$  represent the plant dynamics and the controller for both actuators, respectively. A coupling factor K is defined by

$$K = \frac{1 + C_{PZT} \tilde{G}_{PZT}}{1 + C_{PZT} G_{PZT}}$$
(13)

where  $\hat{G}_{PZT}$  is a model of the PZT actuator. An obvious choice for  $\hat{G}_{PZT}$  would be the 20th order model depicted in Fig.5. However, to limit the complexity of the controller,  $\hat{G}_{PZT}$  is approximated by a simple DC gain  $g_{PZT}$ . The higher frequency resonance modes of the PZT do not have a significant impact on  $S_{VCM}$  because of a high frequency roll-off that is included in  $C_{VCM}$ . Hence,  $K \approx 1$  and both control loops can be decoupled and designed separately.

 $C_{PZT}$  is designed as a band pass filter including a notch filter to suppress the micro-actuator (sway) mode [22] at 17 kHz. Thereafter  $C_{VCM}$  is designed containing a low pass filter approximating an integrator, a second order lead lag compensator and a high frequency roll-off. The actual dual-stage controller  $C_{DS}$  in a classical control loop definition yields

$$C_{DS} = \begin{bmatrix} (1 + g_{pzt}C_{PZT})C_{VCM} \\ C_{PZT} \end{bmatrix}$$
(14)

The dual-stage controller is depicted as the solid lines in Fig. 8 where the left plot shows the actual VCM controller  $(1 + g_{pzt}C_{PZT})C_{VCM}$  and the right plot shows the micro-actuator controller  $C_{PZT}$ .

# C. $H_{\infty}$ loop shaping controller design

In addition to the sensitivity decoupling controller that is designed using loop shaping techniques only, a combined approach is applied that uses loop shaping and  $H_{\infty}$  optimal control design via  $H_{\infty}$  loop shaping [19], [20]. Figure 7 shows the main principle. Information on the  $H_{\infty}$  loop shaping algorithm is given in [21]. The principle steps of the  $H_{\infty}$  loop shaping algorithm are:

First, weighting filters  $W_{VCM}$  and  $W_{PZT}$  are designed for both actuator models that represent the shape of the optimal controllers to be estimated. Then, a 4-block  $H_{\infty}$  control problem is formulated and used to minimize control signal peaking and error rejection peaking. Given the optimization



Fig. 7.  $H_{\infty}$  loop shaping control structure

constraints, an optimal controller  $C_{DS}$  is computed. Finally, the weighting filters are preserved in  $C_{DS}$ .

We define the weighted plant  $G_W$  (dotted box in Fig. 7) as

$$G_W = \begin{bmatrix} W_{VCM} & 0\\ 0 & W_{PZT} \end{bmatrix} \begin{bmatrix} G_{VCM}\\ G_{PZT} \end{bmatrix}$$
(15)

The weighting functions are defined by

$$W_{VCM} = \frac{1}{K_{VCM}} \frac{\tau_1 s + 1}{\tau_2 s + 1} \frac{1}{\tau_3 s + 1}$$

$$W_{PZT} = \frac{R_g}{K_{PZT}} \frac{s}{\tau_4 s + 1} \frac{1}{\tau_5 s + 1}$$
(16)

where the design parameters are given by  $\frac{1}{\tau_1} = 2\pi \cdot 200$ ,  $\frac{1}{\tau_2} = 2\pi \cdot 1$ ,  $\frac{1}{\tau_3} = 2\pi \cdot 5000$ ,  $\frac{1}{\tau_4} = 2\pi \cdot 10$ ,  $\frac{1}{\tau_5} = 2\pi \cdot 800 \frac{\text{rad}}{\text{s}}$  and  $R_g = 5$ . The gains  $K_{VCM}$  and  $K_{PZT}$  are adjusted in such a way that the 0-dB crossover frequency of the weighted plants are located at 500 Hz, respectively, and  $R_g$  is defined as the relative gain of the PZT with respect to the VCM at the crossover frequency. The  $H_\infty$ -norm of the closed-loop transfer function  $T(G_W,C_{DS})$ , defined by

$$T = \begin{bmatrix} G_W \\ I \end{bmatrix} \begin{bmatrix} I + C_{DS} G_W \end{bmatrix}^{-1} \begin{bmatrix} C_{DS} & I \end{bmatrix}, \quad (17)$$

is analytically minimized using normalized coprime factorization and a Nehari extension [21]. Since the calculated controller is of high order (on the order of the plant), a closed-loop reduction routine that subdivides the high order controller into its low order components is applied. A 10th order stable approximation was obtained and is shown as the dashed lines in Fig. 8.



Fig. 8. Comparison SDM and  $H_{\infty}$  loop shaping controller

## D. Controller Evaluation

To evaluate the performance of the designed controllers, the closed loop feedback connection is simulated. The sensitivity functions for both controllers are shown in Fig. 9. The cross-over frequency is nearly the same. However,



Fig. 9. Comparison of closed loop error rejection (sensitivity function) -  $H_\infty$  loop shaping controller and sensitivity decoupling method controller

the  $H_{\infty}$  controller shows a better disturbance rejection for lower frequencies than the SDM controller. Another common performance evaluation is a step function as an input representing either a high frequency disturbance or a short track seek. A step size of 100 nm relates to a track pitch of 250 ktpi in a hard disk drive. Figure 10 shows the simulated response to a step input for both controllers, the control signal for the VCM and the PZT. Furthermore, the individual distribution of the VCM and the PZT to the total displacement is simulated and shown in Fig. 11.



Fig. 10. Simulation of step response -  $H_{\infty}$  loop shaping controller and sensitivity decoupling method controller



Fig. 11. Simulated displacement for VCM and PZT

Here, the SDM controller (solid line) yields almost the same total head displacement as the  $H_{\infty}$  controller (dashed line), although the individual contributions of each actuator are quite different. We observe that the SDM controller settles slightly faster than the  $H_{\infty}$  controller. Also, the maximum value of the control signal and the overshoot are smaller for the SDM controller. Further performance measures are given in Table I.

TABLE I Comparison sensitivity decoupling method (SDM) and  $H_{\infty}$ Loop shaping control design

	SDM	$H_\infty$ loop shaping
gain margin	6 dB	6 dB
phase margin	54 degrees	35 degrees
overshoot	22%	20%
10% settling time	0.175 ms	0.275 ms
crossover frequency	$\approx 2.37 \mathrm{kHz}$	$\approx 2.32 \mathrm{kHz}$
control signal level		
$\ u_{\rm VCM}\ _{\infty}$	5 mV	10 mV
$\ u_{\mathrm{PZT}}\ _{\infty}$	5.1 V	4.7 V

#### IV. CONTROLLER IMPLEMENTATION

The controller was implemented at a sampling frequency of 40 kHz. A 100 Hz square wave reference signal was applied representing a number of step functions. The measurement for the SDM controller is shown in Fig. 12. Each rise and fall in the reference signal (indicated by black arrows) is considered as a step and a trigger. Hence, timebased averaging can be applied (see Fig. 13). Numerous oscillations are observed in the averaged measurement. The unaveraged measurement of the  $H_{\infty}$  controller implementation is shown in Fig. 14. Looking at the averaged step response (Fig.15), one can observe the same oscillations as in the SDM controller measurement.

The major oscillations in both controller implementations occur at about 2 kHz and 3.5 kHz. Furthermore, the control signals show the frequencies of the HDD spindle speed (167 Hz) and Eigen frequencies. It is conjectured that numerous repeatable (non-stochastic) disturbances that are not affected by time-based averaging cause the vibrations.

## V. CONCLUSION

A hard disk drive with dual-stage-suspensions was modified to allow open loop FRF measurements of both servo actuators without having access to the PES. A discrete-time



Fig. 12. Implemented sensitivity decoupling method controller for a square wave reference input



Fig. 13. Head position and control signals for implemented SDM controller (averaged)

modeling algorithm based on frequency response function measurements was proposed. Two different dual-stage trackfollowing controllers were designed using classic loop shaping techniques combined with modern  $H_{\infty}$  control problem algorithms. Both controllers show similar servo performance. However, the  $H_{\infty}$  controller shows a better disturbance rejection than the SDM controller for low frequencies which is due to a low gain in the VCM controller for low frequencies (see Fig.8). Also, the  $H_{\infty}$  approach does not use notch filters, and, thus, is more robust than the SDM controller. Since the optimization routine is constrained by the pre-defined parameters in the weighting functions different weighting functions might result in a better controller performance of the  $H_{\infty}$  controller.

Both, model estimation and optimized controller design



Fig. 14. Implemented  $H_{\infty}$  loop shaping controller for a square wave reference input



Fig. 15. Head position and control signals for implemented  $H_{\infty}$  loop shaping controller (averaged)

based on predefined controller shape filters can be implemented in the hard disk drive firmware. Since actuator dynamics could be a function of tolerances during manufacturing, the drive could perform a controller calibration itself, and, thus, could improve the servo performance and the TMR budget. The different controllers designed in this study were implemented in the HDD and showed a stable feedback control. Small differences between measurement and simulation were observed that are caused by repeatable disturbances.

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